



## I Semester BCA 4 Degree Examination, Nov./Dec. - 2019 MATHEMATICS-I

(Regular)

Paper - (BCA 4)

Time: 3 Hours SECTION - A Maximum Marks: 80

Answer **ALL** of the following questions:

 $(10 \times 2 = 20)$ 

- 1. a) Express  $\frac{2-5i}{2+5i}$  in the form x+iy.
  - b) Simplify  $\frac{\left[\cos A + iSinA\right]^{5}}{\left[\cos 2A iSin2A\right]^{-3}}$
  - c) If the fourth term of A.P. is 15 and whose common difference is -2. Find the 8<sup>th</sup> term of A.P.
  - d) Find the Tenth term of the G.P. 5, 25, 125,.....
  - e) If  $\alpha$  and  $\beta$  are the roots of equation  $2x^2 + 4x 5 = 0$  find the value of  $\alpha + \beta$  and  $\alpha\beta$ .
  - f) State Binomial Theorem.
  - g) P.T.TanA + CotA = SecACosecA
  - h) If  $\vec{a} = 2i 3j k$  and  $\vec{b} = 6i j + 2k$
  - i) Find the distance of the point (3,-4) from the origin.
  - j) Find the equation of straight line given its intercept on axes (3,4).

## **SECTION - B**

Answer any **FOUR** Questions:

 $(4 \times 5 = 20)$ 

- 2. Find the conjugate of the complex number and express it in the form  $a+ib \frac{2-i}{2+i} + \frac{1+3i}{1-3i}$
- 3. The Third term of G.P. is 12 and the sixth term is 96. Find the sum of 9 terms.
- **4.** Find the 8<sup>th</sup> Term in the expansion of  $\left(2x^2 \frac{3}{x}\right)^{12}$ .



- 5. Find the area of the parallelogram whose adjacent sides are  $\vec{a} = 2i + 3j 5k$  and  $\vec{b} = i + 2j + k$ .
- **6.** Find the equation of the straight line which passes through (3,-4) and (-2,5).

## **SECTION - C**

Answer any **FOUR** Questions:

 $(4 \times 10 = 40)$ 

- 7. a) Simplify:  $\frac{(\cos 3\theta + iSin3\theta)^5(\cos 2\theta iSin2\theta)^3}{(\cos 4\theta + iSin4\theta)^2(\cos 5\theta iSin5\theta)^4}$ 
  - b) Express the complex numbers in the polar form and hence find their modules and amplitude z = 1 + i. (5+5=10)
- **8.** a) In a A.P. the seventh term is 20 and the Thirteenth term is 38. Find the Fourteenth term.
  - b) Find the sum of  $5+55+555+\cdots$  to n terms.

(5+5=10)

- **9.** a) Find the middle term in the expansion of  $\left(\frac{x}{a} \frac{a}{x}\right)^{14}$ .
  - b) If  $\alpha$  and  $\beta$  are the roots of  $3x^2 2x + 1 = 0$  find the value of  $\frac{1}{\alpha} + \frac{1}{\beta}$ . (5+5=10)
- **10.** a) Prove that  $\sqrt{\frac{1-\sin\theta}{1+\sin\theta}} = \sec\theta \tan\theta$ .
  - b) In any Triangle ABC, prove that  $2[bcCosA + caCosB + abCosc] = a^2 + b^2 + c^2$ . (5+5=10)
- 11. a) Show that the points A(2,-4) B(4,-2) and C(7,1) are collinear.
  - b) Find the co-ordinates of the point which divides
    - i. Internally
    - ii. Externally the line joining the points (2,3) and (4,5) in the ratio 1:2. (5+5=10)